A moisture budget perspective of the amount effect

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[1] A stable water isotopologue-enabled cloud-resolving model was used to investigate the cause of the amount effect on the seasonal (or longer) time scales. When the total water (vapor and condensed phase) budget of the precipitating column of air is considered, our results indicate that as convection becomes stronger and the precipitation rate increases, the $\delta D$ of precipitation ($\delta D_p$) depends on the isotopic composition of the converged vapor more than that of surface evaporation. Tests with disabled fractionation from rain evaporation demonstrate that this mechanism does not account for the amount effect as has been previously suggested. If the isotopic content of converged vapor is made uniform with height with a value characteristic of surface evaporation, the amount effect largely disappears, further supporting the dominance of converged vapor in changes to the $\delta D_p$ signal with increasing precipitation. $\delta D_p$ values were compared to the water budget term $E/P$, where $P$ is precipitation and $E$ is evaporation. Results from this comparison support the overall conclusion that moisture convergence is central in determining the value of $\delta D_p$ and the strength of the amount effect in steady state.


1. Introduction

[2] Stable water isotopologues (H$_2$O, HDO, H$_2$O, and H$_2$O) are useful as climate proxies and tracers of the hydrologic cycle. Slight differences in the mass of each water isotopologue changes the saturation vapor pressure of the molecule such that the heavier isotopologues tend to collect in condensed phases, while the light isotopologue accumulates in the vapor phase. This fractionation of the heavy and light molecules leads to variations in their respective ratios in a particular phase of water. Changes in these ratios can provide information about temperature [Jouzel, 2003], precipitation amount [Dansgaard, 1964; Rozanski et al., 1993], and moisture source region [Vuille et al., 2003].

[3] Isotopologue ratios in rainwater samples collected from stations included in the Global Network of Isotopes in Precipitation [International Atomic Energy Agency/World Meteorological Organization, 2006] were analyzed by Dansgaard [1964] who noted that in the subtropics and tropics, isotopically depleted rainfall coincided with higher precipitation amounts. This relationship was termed the “amount effect” and was argued to be caused by the increased removal of heavy isotopologues by rainout as clouds cooled. This relationship was later confirmed by Rozanski et al. [1993], who repeated the analysis by Dansgaard, [1964], but with an additional 30 years of data and specifically focused on tropical marine locations.

[4] More recent studies emphasize the role of the unsaturated downdrafts that both directly and indirectly lead to isotopically depleted rainfall [e.g., Risi et al., 2008a, 2008b; Bony et al., 2008; Kurita et al., 2011]. Processes occurring in the unsaturated downdrafts that alter the isotopic composition of the falling precipitation, namely evaporation and equilibration, are referred to as direct effects. As convection strength intensifies, the precipitation rate, average drop size, and the relative humidity in the downdrafts increase. Larger drops do not evaporate as significantly as smaller drops [Stewart, 1975], and overall evaporation decreases as the relative humidity increases. Since evaporation acts to enrich the drops by preferentially removing the lighter isotopologue, decreased evaporation leads to lighter, more depleted rain and thus the amount effect [e.g., Dansgaard, 1964; Risi et al., 2008a; Bony et al., 2008].

[5] As the relative humidity increases in the unsaturated downdrafts, equilibration becomes the dominant mechanism for isotopologue exchange and acts to bring the rain and the surrounding vapor into equilibrium. When the drop size increases in strong convection, the equilibration time of the drop increases while the residence time of the drop in the boundary layer (BL) decreases, leading to rain that does not equilibrate completely with the surrounding vapor [Lee and Fung, 2008; Ciais and Jouzel, 1994; Lawrence et al., 2004; Field et al., 2010]. These partially equilibrated drops do not become as enriched as drops that reach equilibrium and instead maintain the depleted isotopic signal at the cloud base, producing the observed amount effect.

[6] The indirect influence of unsaturated downdrafts is referred to as downdraft recycling, whereby depleted vapor from the downdrafts is injected into the BL, which feeds the convective system. Downdraft vapor is depleted through efficient equilibration of the precipitation with the surrounding vapor in addition to a decreased fraction of evaporation [Risi et al., 2008a] as well as by subsidence of more depleted vapor from the environment [Risi et al., 2008a; Kurita et al., 2011; Risi et al., 2010]. The more efficient the downdraft recycling, the more depleted the precipitation that is produced by the convective system becomes.

[7] As illustrated above, much work has focused on how the boundary layer, convection, and microphysical processes conspire to produce the observed amount effect as
precipitation rates increase. In contrast, Lee et al. [2007] and Kurita et al. [2009] used Global Climate Models (GCM) and found that the isotopic content of the precipitation is a consequence of moisture source region and transport patterns, which is also supported in a recent study by Aggarwal et al. [2012]. In this work, the authors define a residence time parameter that is implicitly dependent on both temperature and circulation patterns and find that it is positively correlated with δ¹⁸O in precipitation collected from 12 global locations. A second recent study [Kurita, 2013] suggests that the amount effect is related to the degree of organization of convection, with relatively enriched precipitation associated with disorganized convection and more depleted precipitation arising from mesoscale convective systems.

The goal of this work is to present a different interpretation as to the cause of the amount effect. In contrast to previous work that studied separate budgets of vapor and condensate [e.g., Risi et al., 2008a; Kurita, 2013], we focus on the total column water (vapor plus condensate) budget of the precipitating column. In regions of deep convection where $P \geq E$, this budget has two sources, surface evaporation and moisture convergence, and a single sink, precipitation. We propose that the anticorrelation between the $\delta D$ in precipitation ($\delta D_p$) and precipitation amount is largely a result of isotopically depleted vapor converging in the lower and middle troposphere with smaller contributions from surface evaporation. This approach is similar to that of Lee et al. [2007] who clearly identify the relationship between $P$ and $E$ and the isotopic composition of precipitation in simulations with an isotope-enabled GCM.

The model used for this study is an isotope-enabled version of the System for Atmospheric Modeling (SAM), version 6.7 [Khairoutdinov and Randall, 2003] and will hereafter be referred to as IsoSAM. Isotopologue physics is implemented in the model by incorporating phase changes of the heavy water isotopologues into the Lin microphysics scheme of the Weather and Research Forecasting model, version 3.1 [Skamarock and Klemp, 2008]. This version of the Lin microphysics scheme closely resembles that of Lin et al. [1983] and is a single-column bulk scheme that performs mixed phase saturation adjustment and does not allow for supersaturation with respect to ice at temperatures below $-40^\circ$C [Blossey et al., 2010]. IsoSAM incorporates the heavy isotopologues (HDO and H$_2$¹⁸O) by replicating the transformation processes of H$_2$¹⁸O. Fractionation is set to occur during water phase changes, which is described in detail in Blossey et al. [2010, Appendix B].

For all of the experiments, IsoSAM is configured as a three-dimensional cloud-resolving model using a radiative-convective equilibrium (RCE) framework over an ocean surface. The simulations run for 500 days with an initial sea surface temperature (SST) of 301.15 K on a domain that is 128 km × 128 km with periodic boundary conditions and 64 vertical levels. The weak temperature gradient approximation (WTG) is implemented once the model reaches equilibrium, making it possible to diagnose the vertical velocity and precipitation associated with the changes in SST and prescribed temperature profiles [Sobel and Bretherton, 2000]. Results presented here use the damped gravity wave approach of Kuang [2008] and Blossey et al. [2009] to compute the pressure velocity perturbation. Simulations using the approach of Sobel and Bretherton [2000] produce similar results and will not be presented here for brevity. Bony et al. [2008] found using WTG to diagnose the vertical velocity in a RCE framework capable of reproducing $\delta D_p$ values close to those in observations.

Tendencies of moisture and temperature (represented here by $\chi$) due to large-scale circulations that cannot be represented in our small periodic domains are calculated using equation (1):

$$\frac{\partial \chi}{\partial t} = \frac{\bar{\chi}}{p} \frac{\partial \bar{\rho w}}{\partial z} \frac{1}{\bar{\rho}} \frac{\partial (\bar{\rho w} \bar{\rho})}{\partial z}, \quad (1)$$

as in Daleu et al. [2012] and Raymond and Zeng [2005] (Figure S1 in supporting information for a depiction of these terms).

The over bar indicates the horizontal average of the variables, and it is assumed that the horizontal wind is either into or out of the column, as represented by the upwind value $\chi^*$. In regions of large-scale divergence ($\frac{\partial \rho w}{\partial z} < 0$), the upwind value of $\chi^* = \bar{\chi}$, while in regions of large-scale convergence ($\frac{\partial \rho w}{\partial z} > 0$), $\chi^* = \chi^{ref}$. The model reaches equilibrium ($\sim$ day 60) before reference profiles are calculated (days 100–120); after which point WTG is initiated. The SST is increased by 0.5 K increments approximately every 45 days starting at day 255, providing six SST regimes ranging from 301.15 K to 303.65 K for our analysis. In all of the experiments, heavy isotopologues in the atmosphere are initialized at 0, such that the ocean is assumed to serve as an infinite source of all water isotopologues and heat.

2. Model and Experiments

2.1. Model Setup

The model used for this study is an isotope-enabled version of the System for Atmospheric Modeling (SAM), version 6.7 [Khairoutdinov and Randall, 2003] and will hereafter be referred to as IsoSAM. Isotopologue physics is implemented in the model by incorporating phase changes of the heavy water isotopologues into the Lin microphysics scheme of the Weather and Research Forecasting model, version 3.1 [Skamarock and Klemp, 2008]. This version of the Lin microphysics scheme closely resembles that of Lin et al. [1983] and is a single-column bulk scheme that performs mixed phase saturation adjustment and does not allow for supersaturation with respect to ice at temperatures below $-40^\circ$C [Blossey et al., 2010]. IsoSAM incorporates the heavy isotopologues (HDO and H$_2$¹⁸O) by replicating the transformation processes of H$_2$¹⁸O. Fractionation is set to occur during water phase changes, which is described in detail in Blossey et al. [2010, Appendix B].

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shown in terms of HDO, since $\delta^{18}O$ and $\delta D$ values are generally proportional, and showing results for both isotopologues would be redundant.

[15] Two sensitivity studies are performed to identify the key contributor to changes in $\delta D_p$ with increasing precipitation. First, an evaporation test disables fractionation associated with rain evaporation and equilibration. The vapor produced by rain evaporation has the same isotopic composition as the rain itself and thus ensures that there is no preferential removal of the lighter isotopologue. This is done by setting the isotopic content of the evaporation flux to be equal to the ratio of HDO rain to H$_2$O rain multiplied by the amount of H$_2$O water evaporated from the raindrop. Prohibiting fractionation during rain evaporation can be expected to prevent the rain from becoming increasingly heavier as the rain evaporation takes place in relatively dry air and instead should cause it to become lighter compared to the control case.

[16] Second, we performed an experiment with a reference water vapor profile that has a uniform isotopic composition with height ($\delta D_{ref}^{ref}$). The uniform reference vapor profile is set to be $-23%0$, representing the $\delta D_v$ of the evaporated surface flux in the control case. As vapor generally becomes more depleted with height, using the uniform $\delta D_{ref}^{ref}$ will tend to make the isotopic composition of converged vapor and the resulting precipitation isotopically more enriched relative to the control simulation. However, in simulations where $P/\Delta E$ and there is no net import of vapor to the column, the effect of changing $\delta D_{ref}^{ref}$ will likely be small.

### Table 1. Control Run Values and Uniform $\delta D_{ref}^{ref}$ Test Values\(^a\)

<table>
<thead>
<tr>
<th>SST</th>
<th>$\delta D_{Bl,Evap}$</th>
<th>Evap</th>
<th>BL</th>
<th>$\delta D_p$</th>
<th>Prec</th>
<th>Conv Vap</th>
<th>$\alpha_{eff}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>301.15 K</td>
<td>$-25%0$</td>
<td>3.1 mm/day</td>
<td>$-93%0$</td>
<td>$-23%0$</td>
<td>3.0 mm/day</td>
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<td>1.08</td>
</tr>
<tr>
<td>301.65 K</td>
<td>$12%0$</td>
<td>3.6 mm/day</td>
<td>$-116%0$</td>
<td>$-50%0$</td>
<td>6.1 mm/day</td>
<td>$-160%0$</td>
<td>1.07</td>
</tr>
<tr>
<td>302.15 K</td>
<td>$29%0$</td>
<td>4.0 mm/day</td>
<td>$-130%0$</td>
<td>$-66%0$</td>
<td>8.9 mm/day</td>
<td>$-152%0$</td>
<td>1.07</td>
</tr>
<tr>
<td>302.65 K</td>
<td>$33%0$</td>
<td>4.4 mm/day</td>
<td>$-138%0$</td>
<td>$-74%0$</td>
<td>11.4 mm/day</td>
<td>$-147%0$</td>
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</tr>
<tr>
<td>303.15 K</td>
<td>$35%0$</td>
<td>5.1 mm/day</td>
<td>$-143%0$</td>
<td>$-79%0$</td>
<td>14.2 mm/day</td>
<td>$-144%0$</td>
<td>1.07</td>
</tr>
<tr>
<td>303.65 K</td>
<td>$32%0$</td>
<td>5.5 mm/day</td>
<td>$-146%0$</td>
<td>$-83%0$</td>
<td>16.1 mm/day</td>
<td>$-142%0$</td>
<td>1.07</td>
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\(^a\)Table includes $\delta D_v$ of surface evaporation, surface evaporation rate, $\delta D_v$ of boundary layer (lower 50 mb), $\delta D_p$, precipitation rate, and $\delta D$ of converged vapor as well as the effective fractionation factor ($\alpha_{eff} = R_{Bl,Evap}/R_{Bl}$) for the control and uniform $\delta D_{ref}^{ref}$ test averaged for each SST regime. Converged vapor is near zero for the first SST regime, and thus, no $\delta$ value has been calculated.
3. Model Results

3.1. Control Case

[17] In the control run, the output produces an amount effect comparable to observations, though more depleted by as much as 40% for the highest precipitation rates (see Figure 1, left and Table 1). The results are also in agreement with those of previous work using a similar setup with a single-column model [Bony et al., 2008]. Since the simulation is run in RCE with an idealized representation of the large-scale circulation, one cannot expect to replicate observations exactly.

3.2. Evaporation Test

[18] Decreased rain evaporation has been argued to be a key mechanism of the amount effect [e.g., Dansgaard, 1964; Risi et al., 2008a; Bony et al., 2008; Lee et al., 2011], and here we test this theory in our model framework by disabling fractionation during rain evaporation (i.e., vapor evaporated from rain has the same isotopic content as the rain itself).

[19] The blue points in Figure 1 (left) show the output from this experiment and due to the restriction on the rain evaporation, the rain becomes slightly more depleted than the control run. We note that the change is small between the two runs and the difference decreases as the SST increases, which is expected with increased precipitation rates and thus decreased evaporation. This leads to a smaller difference in the $\delta D_p$, while the opposite is true in lower precipitation rate cases, when rain evaporation will be greater.

[20] These small changes of $\delta D_p$ values from the control run as well as the fact that the amount effect is still present indicate that rain evaporation does not appear to contribute as greatly to the amount effect as has been previously assumed. Had the evaporation been an essential part of the amount effect, disabling this fractionation process would have more of an impact on the amount effect.

3.3. Uniform $\delta D_p$ Profile Test

[21] This test demonstrates how the observed $\delta D_p$ signal results from the relative contributions of the various vapor sources of distinct isotopic contents. Here the isotopic content of the environment, and thus converged vapor, is set to have the same $\delta D$ value as surface evaporation. The output from this test (green points in Figure 1, left) indicates, as expected, that the amount effect essentially disappears, with $\delta D_p$ values oscillating around $-24\%$ despite increases in the precipitation rate.

4. Discussion

4.1. Amount Effect and Moisture Convergence

[22] We present an interpretation that explains the amount effect when considering the total water (vapor plus condensate) budget of the precipitating column. Here surface evaporation and large-scale moisture convergence are the two sources of atmospheric water, and convergence of vapor is most important in determining the value of $\delta D_p$ as convection strengthens. This interpretation is in accordance with Kurita [2013] who finds that an increasing fraction of stratiform (as opposed to convective) precipitation [e.g., Houze, 2004] is associated with more depleted rainfall. As the inflow to stratiform regions occurs mainly in the midtroposphere [Mapes and Houze, 1995] where the vapor is more depleted than in the boundary layer, moisture import to these regions will reinforce the amount effect.

[23] The moisture import could potentially alter the influence of the BL vapor because of variations in the isotopic content of the converged vapor, due to changes in the structure of the vertical velocity profile. Back and Bretherton [2006] analyzed data from ERA40 and found that vertical velocity profiles in the East Pacific tend to be bottom heavy while in the West Pacific are top heavy. In the present study, the large-scale vertical velocity $\overline{w}$ peaks in the upper troposphere for all but the coldest SST (Figure S2) so that moisture convergence occurs over a deep layer. Since the profile of $\delta D$ becomes more depleted with height, the level of strongest convergence will influence the composition of the converged vapor; however, comparing how $\delta D$ changes according to different vertical velocity profiles is outside the scope of this paper.

4.2. Amount Effect and Moisture Residence Time

[24] We define a budget parameter, $\overline{E}$, to correlate with $\delta D_p$, similar to work by Lee et al. [2007]. The distinction between $\overline{E}$ and residence time [Aggarwal et al., 2012] is important for paleoclimate studies that use the correlation between $\delta D_p$ and such parameters to estimate regional and local precipitation patterns. Held and Soden [2006] found that total precipitable water scales with the Clausius Clapeyron (CC) equation and varies by 7% per degree Kelvin change, while $P$ (and therefore $E$) is much weaker than the CC scaling and only changes about 2% per degree Kelvin.

[25] The value of $1 - \overline{E}$ will indicate the relative contribution of moisture convergence (and horizontal advection of upstream air into the domain, which is neglected here) in the steady state system. When $P = E$, converged vapor makes no net contribution to surface precipitation, which appears to be the case for the first SST regime (blue point in Figure 1, right). $P \gg E$ indicates that converged vapor is the primary source for precipitation. Performing the calculations with the output from the control run, we find that as the SST increases and convection becomes stronger, $\overline{E}$ decreases, implying that converged vapor is making up the bulk of the precipitation.

4.3. Amount Effect and Boundary Layer Vapor

[26] Table 1 includes the $\delta D$ values of the various vapor sources and the precipitation for the control run and uniform $\delta D_p$ test, respectively. Across the range of SSTs and precipitation rates in our experiments, the isotopic ratios of the boundary layer vapor and precipitation change together, with an effective fractionation factor $\alpha_{eff} = R_p/R_{eq} = 1.07 – 1.08$ that is roughly fixed and close to the equilibrium fractionation factor $\alpha_{eq} = 1.08 – 1.09$ [Majoube, 1971] at temperatures within the boundary layer. Figure S3 depicts the relationship between $\delta D_{bl}$ and $\delta D_p$ across the range of SSTs in our experiment. Kurita [2013] found a similar relationship in observations of the isotopic content surface vapor and precipitation, as the fit in his Figure 8 corresponds to $\alpha_{eq} = R_p/R_{vap} = 1.07 – 0.25*(R_{vap} – 0.9) \sim 1.05 – 1.08$ for the value of $R_{vap}$ in that figure. Note that in our experiment, there is more scatter and a different slope in the relationship between $R_{vap}$ and $\delta D_p$ for a given SST and precipitation regime than is found across the whole range of SSTs and precipitation rates.
The relative roles of post-condensation exchange, downdraft recycling, and environmental subsidence in maintaining the relationship between $R_{hi}$ and $R_{ph}$ across the wide range of precipitation rates is secondary to the role of converged vapor in maintaining steady state and is thus beyond the scope of this study but is planned for future work.

5. Conclusions

The goal of this study is to demonstrate that increasing convergence of water vapor is the key contributor to the observed amount effect in steady state. While a range of processes, such as entrainment, condensation, evaporation, and equilibration, are involved in producing the isotopic composition of rain, the moisture budget perspective offers a convenient overall constraint that the system must adjust to satisfy when in steady state and that offers a simple interpretation of the amount effect. We have shown that the decrease in rain evaporation and equilibration will contribute to the depletion, but the role of these processes is small compared to convergence of vapor in a steady state scenario. Results do suggest a secondary role of the boundary layer vapor, whose isotopic composition is found to be well correlated with that of precipitation across the wide range of precipitation rates in this study. However, the precise role of the boundary layer and convective processes in maintaining this relationship is outside the scope of this study.

We have also proposed the parameter $\frac{E}{P}$ for comparison with $\delta D_p$. This variable indicates the strength of the hydrological cycle and provides information about the local water budget, making it possible to diagnose the relative contributions of vapor sources for precipitation in steady state. Knowing where moisture is coming from is important since a change in the moisture sources of convection could drastically alter the value of $\delta D_p$.

The results presented support our hypothesis, though there are some caveats that should be addressed further in future work. As horizontal advection was neglected during our budget calculations, we intend to include this term in future work with an isotope-enabled version of the Super-Parameterized Community Atmosphere Model. Also, our results only address steady state and therefore represent the amount effect on monthly and seasonal time scales. In some instances, the amount effect has been observed on the time scale of single storms [e.g., Dansgaard, 1964; Nijtschou et al., 1999; Yoshimura et al., 2003], which the current results do not address. The arguments presented here could be applicable to individual storms, but further testing is required to confirm this.

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